

Answers to Selected Problems: Chapter 10

10.4

2.

$$\varepsilon(t) = \sigma_o \left\{ \ln(t+1) + B[(t+1)\ln(t+1) - t] \right\}$$

3.

(ii) b

(iii) no instantaneous elastic recovery; has permanent deformation

$$(iv) \varepsilon(t) = t^2 - t + (1 - e^{-2t})/2$$

$$4. \varepsilon(t) = \begin{cases} \frac{\sigma_c}{Et_1} \left\{ t - (\eta/E)(1 - e^{-(E/\eta)t}) \right\}, & 0 < t < t_1 \\ \frac{\sigma_c}{Et_1} \left\{ (2t_1 - t) + (\eta/E)(1 + e^{-(E/\eta)t}(1 - 2e^{(E/\eta)t_1})) \right\}, & t_1 < t < t_2 \\ \frac{\sigma_c}{Et_1} (\eta/E)e^{-(E/\eta)t} (1 - e^{(E/\eta)t_1})^2, & 2t_2 < t \end{cases}$$

10.5

$$2. J(t) = \frac{t}{\eta_1} + \frac{1}{E} (1 - e^{-(E/\eta_2)t})$$

10.6

1.

$$\begin{aligned} \varepsilon(t) &= \sigma_o (J_1 \cos \omega t + J_2 \sin \omega t) \\ &= \sigma_o \left(\frac{E}{E^2 + (\eta\omega)^2} \cos \omega t + \frac{\eta\omega}{E^2 + (\eta\omega)^2} \sin \omega t \right) \end{aligned}$$

At low frequencies, it behaves like an elastic material.